

Typing Tools for Typeless Stack Languages

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Abstract. Many low-level runtime engines and virtual machines are stack based - instructions take parameters from the stack and leave their results on the stack. Stack language is a common name for several languages used to program stack based (virtual) machines - like CLR, JVM, Forth, Postscript, etc. We chose the Forth language as an example to represent the class of stack languages, partially because this language is typeless, partially because there exists a big amount of industrial legacy Forth code that needs to be validated.

Usually applications that take advantage of stack machines are minimalistic and designed to run on restricted environments like electronic devices, smartcards, embedded systems, etc. Sometimes these components are used to build safety critical systems where software errors are inadmissible. Type checking allows to locate possible errors of stack usage that most often occur in stack language programs. Limited resources give preference to a static solution - run-time type information is expensive to manage and quite useless in turnkey applications. Static type checking is based on a type system that is introduced here for originally typeless stack languages. This external type system is flexible enough to perform several tasks. Static program analysis can be used both for finding errors and performing useful transformations on programs (optimization, parallelization, etc.).

In this paper a type system to perform the so called must-analysis is described that allows to locate the stack language code where the strong stack discipline is violated. Experimental implementation of the analysis framework is written in Java.

Keywords: *Type Systems, Stack Languages, Program Analysis*

1 Introduction

Program analysis became popular in the world of embedded systems and safety critical applications where more resources are used to avoid software errors than in usual office software business. Many run-time properties of a program can be estimated statically using some kind of abstract interpretation [1]. Good analysis produces reasonable amount of warnings about suspicious passages in the program, so the human programmer can check these lines and make improvements to the software.

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Unfortunately, analysis can be very resource-consuming, in some cases even small pieces of software embedded in some device take a lot of computing power to analyze. Number of program states to explore grows very fast for precise analysis, to keep it under control some approximation is needed to glue similar states into a single one. On the other hand, the analysis still has to produce valuable results.

The so called control flow graph of a program describes all possible execution paths as a finite structure. The program state is coupled with the node (sometimes with the edge) of the control flow graph. The typical analysis problem is “What is known about . . . in program point . . .?”. There are two different kinds of statements: first, when a property must hold for all possible execution paths, and second, when a property may hold for some particular execution (there is no guarantee that it does not hold). Sometimes the must-analysis finds less properties guaranteed than there actually exist, similarly the may-analysis sometimes finds more properties than these that actually might hold. It is important to use safe, conservative approximations, because a precise result in this area is usually hard or impossible to compute.

Classical data flow analysis concentrates on memory - program state is described via set of variables and analysis keeps track on variable usage and variable updates. We can find out uninitialized variables, live variables, available expressions, reaching definitions, very busy expressions, etc. Good introduction to program analysis is made in book [2].

In case of stack languages the memory state is a secondary issue, it is more important to check the usage of stack(s). For example, a common mistake is to write alternative program branches with different stack effects (it is not easy to discover this bug if some branch is hardly ever executed).

In this paper we introduce some new ideas on static analysis of stacks, these ideas are partially implemented as a set of Java classes. Java is used as an available multi-platform tool, we intend to use the existing Java API to produce some Forth-targeted tools (like validator and editor that supports the strong stack discipline).

The formalism is mainly used to give a precise definition to the rules that Forth programmers know intuitively. On the other hand, it is a short way to explain these more than thousand lines of code written to implement the basic operations.

2 Typing rules

Original stack effect calculus is introduced in [3], related work by Bill Stoddart and Peter Knaggs is published in [6], few other works are referred in [5]. From the viewpoint of program analysis it is important to mention an attempt to formalize multiple stack effects for control structures in [4]. This approach did not lead to implementation of practical analysis tools, mainly because the sets of stack effects grew fast and were costly to manage. Instead of asking “What this program might do?” (interesting, but costly and impracticable question) we

now prefer to ask "Why this program does not do what it has to do?" (locating a suspicious passage).

The following framework is oriented to the must-analysis. There are theoretical considerations to restrict ourselves to this type of analysis: the set of stack effects as defined originally (polycyclic monoid) is a semilattice (each subset has a greatest lower bound *glb* but does not necessarily have a least upper bound). Only the subset of idempotents is a lattice (e is an idempotent iff $e = e \cdot e$).

In this paper the derivation rules are used to express the composition and *glb* of stack effects. There are two main constructs and one strong assumption:

- 1) composition (multiplication) of stack effects describes a linear segment of a program,
- 2) greatest lower bound of stack effects describes merging of alternative branches of a program,
- 3) body of a program loop is described by an idempotent stack effect (the stack state does not change).

Let us introduce some notation for stack effects.

t, u, \dots - possible types of data stack items.

$t \leq u$ - t is subtype of u (t is more exact) or equal to u
(subtype relation is transitive).

$t \perp u$ - t and u are incompatible types.

t^i - type symbol with wild-card index
(wild-card index i is unique for elements of "the same type").

a, b, c, d, \dots - type lists that represent the stack state (top right).

$s = (a \rightarrow b)$ - stack effect (a - stack state before the operation, b - after).

1 - empty effect (no inputs, no outputs), top of lattice of idempotents.

0 - zero effect (error, type conflict), bottom of lattice of idempotents.

$(a \rightarrow b) \cdot (c \rightarrow d)$ - composition of two stack effects (defined later).

x, y, \dots - sequences of stack effects.

y , where $u^j := t^k$ - substitution of u^j to t^k
(all occurrences of u^j in all type lists of sequence y are replaced by t^k)
 k is unique index over y .

$(a \rightarrow b) \sqcap (c \rightarrow d)$ - *glb* of two stack effects (defined later).

$r = \sqcap^* s$ - greatest idempotent r smaller or equal to s , zero is allowed
($r \cdot r = r$ and $r \leq s$).

α, β, \dots - sequences of operations (linear programs).

$s(\alpha)$ - stack effect of sequence α .

Rules for composition

These rules describe evaluation of sequence of stack effects. Whenever a type clash occurs the result is zero. When two types (coming from different contexts) for the same stack item are compared the more exact type “wins” and this information is spread to whole evaluated part of the sequence (denoted by x).

$$\frac{x \cdot \mathbf{0}}{\mathbf{0}}$$

$$\frac{\mathbf{0} \cdot y}{\mathbf{0}}$$

$$\frac{x \cdot (a \rightarrow bt) \cdot (cu \rightarrow d), \text{ where } t \perp u}{\mathbf{0}}$$

$$\frac{x \cdot (a \rightarrow b) \cdot (\rightarrow d)}{x \cdot (a \rightarrow bd)}$$

$$\frac{x \cdot (a \rightarrow) \cdot (c \rightarrow d)}{x \cdot (ca \rightarrow d)}$$

$$\frac{x \cdot (a \rightarrow bt^i) \cdot (cu^j \rightarrow d), \text{ where } t \leq u}{x \cdot (a \rightarrow b) \cdot (c \rightarrow d), \text{ where } t^i := t^k \text{ and } u^j := t^k}$$

$$\frac{x \cdot (a \rightarrow bt^i) \cdot (cu^j \rightarrow d), \text{ where } u \leq t}{x \cdot (a \rightarrow b) \cdot (c \rightarrow d), \text{ where } t^i := u^k \text{ and } u^j := u^k}$$

Example

Let us have the following toy type system that represents a fragment of the Forth programming language:

```
a-addr < c-addr < addr < x
flag < x
char < n < x
```

Using these types and wild-cards we can introduce hypothetical stack effects:

```
DUP ( x[1] -- x[1] x[1] )
DROP ( x -- )
SWAP ( x[2] x[1] -- x[1] x[2] )
ROT ( x[3] x[2] x[1] -- x[2] x[1] x[3] )
OVER ( x[2] x[1] -- x[2] x[1] x[2] )
PLUS ( x[1] x[1] -- x[1] )
  polymorphic "plus", arguments have to have the same type
+ ( x x -- x )
@ ( a-addr -- x )
! ( x a-addr -- )
C@ ( c-addr -- char )
C! ( char c-addr -- )
DP ( -- a-addr )
O= ( n -- flag )
NOT ( x -- x )
```

Now let us apply the rules to some example programs

OVER OVER PLUS ROT ROT PLUS !
 evaluates to (a-addr[1] a-addr[1] --)

On the other hand, the following program has type conflict in it
 OVER OVER PLUS ROT ROT PLUS C!

It is suggested to play with some more examples to understand how the rules work (author also has an implementation for this set of stack effects).

Rules for greatest lower bound

To join the type information from different alternative branches of a program we need an operation \sqcup of finding the least upper bound of finite set of effects. As mentioned before, this approach does not work well. Instead, we formulate a different problem - what are the weakest conditions to make all branches equal? This problem can be solved using greatest lower bound operation \sqcap . We approximate the branching control structure as a whole by *glb* of all the branches.

$$\frac{s \sqcap \mathbf{0}}{\mathbf{0}} \qquad \frac{r \sqcap s}{s \sqcap r}$$

If there exist type lists $a_1, a_2, a_3, b_1, b_2, b_3, c_1, c_2, c_3$ such that for all elements of the lists these subtyping relations hold element-wise

$$a_3 = \min(a_1, a_2)$$

$$b_3 = \min(b_1, b_2)$$

$$c_3 = \min(c_1, c_2)$$

then the following rule is applicable, in all other cases the result is zero.

$$\frac{(c_1 a_1 \rightarrow c_2 b_1) \sqcap (a_2 \rightarrow b_2)}{(c_3 a_3 \rightarrow c_3 b_3)}$$

If a set of effects has a non-zero *glb* r then all effects in this set "do the same thing", r is just the most exact description of it (having longest lists and most exact types). In case it is impossible to force effects to be comparable (in sense of finding a common predecessor for them) the *glb* is zero (zero is less or equal to any stack effect).

We also introduce the following notation that is useful for loops:

$$\sqcap^* s = s \sqcap (s \cdot s)$$

The result of this operation is an idempotent element that most precisely describes the loop body s .

Example

ROT and @ from the previous example have *glb*

```
( a-addr[1] a-addr[1] a-addr[1] -- a-addr[1] a-addr[1] a-addr[1] )
```

C@ and @ have *glb*

```
( a-addr -- char )
```

Rules for control structures

In [4] we introduced some rules for may-analysis like the following (we do not reproduce all the rules here but just two most characteristic examples):

$$\frac{s(\text{ IF } \alpha \text{ ELSE } \beta \text{ THEN })}{[(\text{true} \rightarrow) \cdot s(\alpha)] \sqcup [(\text{false} \rightarrow) \cdot s(\beta)]}$$

$$\frac{s(\text{ BEGIN } \alpha \text{ WHILE } \beta \text{ REPEAT })}{\sqcup^*[s(\alpha) \cdot (\text{true} \rightarrow) \cdot s(\beta)] \cdot s(\alpha) \cdot (\text{false} \rightarrow)}$$

These rules describe the semantics of control structures but are hard to use for practical analysis. Informally, words IF and WHILE consume a Boolean flag (the top of the data stack) to decide which branch to choose, other control words are used as structure boundaries.

Let us introduce some new less exact rules in must-analysis style.

$$\frac{s(\text{ IF } \alpha \text{ ELSE } \beta \text{ THEN })}{(\text{flag} \rightarrow) \cdot [s(\alpha) \sqcap s(\beta)]}$$

$$\frac{s(\text{ BEGIN } \alpha \text{ WHILE } \beta \text{ REPEAT })}{\sqcap^*[s(\alpha) \cdot (\text{flag} \rightarrow)] \cdot \sqcap^*s(\beta)}$$

These rules are quite strict about sequences α and β (violating the strong stack discipline implies the zero effect).

Rules for other Forth control structures are similar to these above.

Example

A good exercise is to think about the program:

```
: test IF ROT ELSE @ THEN ;
```

What is the right analysis for this program? Is this program correct?

Hint: we already know the *glb* (ROT, @) from the previous example.

Another good example from [4] uses a while-cycle:

```
: test2 BEGIN SWAP OVER WHILE NOT REPEAT ;
```

`test2` may loop forever in "integer" world, in "Boolean" world it is nearly equivalent to

```
: test3 OR FALSE SWAP ;
```

3 Conclusion

Stack languages are used in embedded and safety critical system engineering where the software testing often incorporates tools for program analysis. The stack based approach induces the need for specific stack analysis methods. Typeless nature of stack languages allured to create an external type system that forms a basis for static type checking.

The rules introduced above allow finding such conditions that guarantee certain behaviour of the program when hold, but probably these conditions force too strong stack discipline (no instructions with multiple stack effects, no branches with different stack effects, no loops that grow or shrink the stack). On the other hand, pointing to the spots where this discipline is violated might help a lot. We already started a pilot project on implementing this analysis to validate some industrial Forth legacy code.

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